

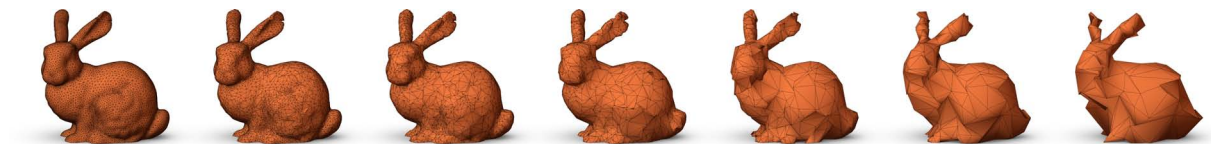
# Growing Cell Structures Learning a Progressive Mesh During Surface Reconstruction – A Top-Down Approach

Tom Vierjahn<sup>1,2</sup>, Guido Lorenz<sup>1</sup>, Sina Mostafawy<sup>1,3</sup>, and Klaus Hinrichs<sup>2</sup>

<sup>1</sup>[rmh] new media GmbH, Cologne, Germany

<sup>2</sup>Visualization and Computer Graphics Research Group, University of Muenster, Germany

<sup>3</sup>Department of Media, FH Duesseldorf University of Applied Sciences, Germany



**Figure 1:** Reconstruction of Stanford Bunny with 20,000 triangles (far left) and the automatically learned level of detail. For each step the number of triangles was halved until reaching 312 triangles (far right).

## Abstract

*Growing Cell Structures (GCS) have been proven to be suitable for surface reconstruction from unstructured point clouds. The reconstructed triangle mesh can be represented compactly as a progressive mesh with integrated level of detail by storing only vertex split operations. However, half-edge collapse operations are used for GCS.*

*In this paper, we present an improvement to a GCS-based surface reconstruction technique by converting a half-edge collapse to a more general vertex removal to create a progressive mesh. We have evaluated the new technique with respect to running time overhead and mesh quality. Results indicate that this technique can be used for efficient surface reconstruction. We will use the presented findings as basis for future research.*

Categories and Subject Descriptors (according to ACM CCS): Computer Graphics [I.3.5]: Computational Geometry and Object Modeling — Curve, surface, solid, and object representations; Geometric algorithms, languages, and systems—

## 1. Introduction

Urban models reconstructed from aerial images play an essential role in different areas, e. g., map creation, surveying or disaster management. In the AVIGLE project [RGW\*10] we are developing an automated reconstruction process using images taken by a swarm of miniature unmanned aerial vehicles [SFS\*11]. A 3D point cloud, obtained by 3D reconstruction from the aerial images [RSH11], forms the input to the subsequent surface reconstruction process. A database server is used as a central storage for all processes.

Since we are expecting very large, dynamic point clouds, growing incrementally due to the acquisition and processing of additional images, we employ a reconstruction algorithm

based on an artificial neural network capable of unsupervised learning. Since transfer of the mesh has been identified as a bottleneck, we improved the reconstruction process in such a way that the resulting mesh is represented compactly as a progressive mesh – without any post processing.

## 2. Related Work

First experiments in the AVIGLE project proved an artificial neural network to be generally usable for surface reconstruction [SFS\*11]. Since our point clouds are dynamic, we have based our algorithm on Growing Cell Structures [Fri93] that iteratively adapt the size of the triangle mesh. [IkJpS03] and [AB10] presented improvements to this algorithm.

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while  $\epsilon_c < \epsilon_r$  do
   $p = \text{random Sample}(\mathbb{P})$ 
   $v_w = \arg \min(\|p - v\|)$ 
   $v'_w = v_w + \alpha_w(p - v_w)$ 
  for all  $v_g \in 1\text{-ring}(v_w)$  do
     $v'_g = v_g + \alpha_g \mathcal{L}_t(v_g)$ 
  if vertex removal is necessary then
    remove  $\mathbb{V}_x = \{v_x \in \mathbb{V} \mid \text{activity}(v_x) \leq \epsilon_r\}$ 
  if vertex split is necessary then
    split  $v_a = \arg \max(\text{activity}(v))$ 
end

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Figure 2: Learning algorithm

A progressive mesh representation [Hop96] of a triangle mesh allows for compact storage and transfer, level of detail and incremental refinement in the visualization process. However, until now, a progressive mesh representation could only be created by post processing.

### 3. Technique

In the AVIGLE project an unstructured set of points  $\mathbb{P}$  representing visible geometry is extracted from aerial images [RSH11]. A 2-manifold triangle mesh  $M = (\mathbb{V}, \mathbb{T})$  consisting of a set of vertices  $\mathbb{V}$  and a set of triangles  $\mathbb{T}$  can be reconstructed from  $\mathbb{P}$  using a technique based on improved Growing Cell Structures (GCS) [IkJpS03]. Finally  $M$  is stored in a database for subsequent visualisation.

#### 3.1. Growing Cell Structures

In GCS  $\mathbb{V}$  can be used as the set of neurons of the artificial neural network learning the shape of  $M$ . Vertex and neuron are used synonymously throughout this paper. For simplicity let  $\mathbb{P}, \mathbb{V} \subset \mathbb{R}^3$ . Nevertheless, this can be extended to  $\mathbb{P}, \mathbb{V} \subset \mathbb{R}^n$  by including color, texture coordinates etc. A tetrahedron is used as the initial topology  $M_0$  of the network.

Learning (cf. fig. 2) terminates if a certain quality criterion  $\epsilon_c$  reaches a predefined threshold  $\epsilon_r$ , e. g., the number of vertices or the average distance of all  $v \in \mathbb{V}$  to all  $p \in \mathbb{P}$ . In each learning step for a randomly chosen signal  $p \in \mathbb{P}$  the neuron  $v_w \in \mathbb{V}$  closest to  $p$  with respect to the Euclidean distance  $\|p - v_w\|$  is determined and moved towards  $p$  according to a learning rate  $\alpha_w$ . To prevent fold-overs and convergence towards local minima Laplacian smoothing  $\mathcal{L}_t$  weighted by  $\alpha_g$  is applied to the neighbors  $v_g$  of  $v_w$ .

After a certain number of iterations a set of inactive neurons  $\mathbb{V}_x$  can be determined that have to be removed from the network by a half-edge collapse. Furthermore, the most active neuron  $v_a$  can be determined representing a region with too few neurons. Thus, an additional neuron has to be added by a vertex split. For the mesh to grow vertex addition has to be triggered more often than vertex removal.

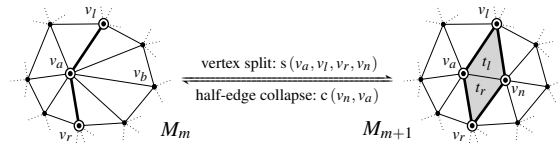


Figure 3: Vertex split  $s$  and half-edge collapse  $c$

#### 3.2. Vertex Split

A new vertex  $v_n$  and two triangles  $t_l$  and  $t_r$  are added to  $M$  by a vertex split  $s$  (cf. fig. 3). Let  $v_b$  denote the end vertex of the longest edge incident to  $v_a$ , then for simplicity  $v_n = \frac{v_a + v_b}{2}$ , but any position inside the triangles to the right of the edge-sequence  $v_r, v_a, v_l$  and incident to  $v_a$  will be suitable. This operation preserves the topological type of  $M$  [HDD\*93].

For any mesh  $M_m = (\mathbb{V}_m, \mathbb{T}_m)$  a vertex split  $s(v_a, v_l, v_r, v_n)$  is unambiguously defined by  $v_a, v_l, v_r \in \mathbb{V}_m$  and the new vertex  $v_n$  as a transformation from  $M_m$  to a new mesh  $M_{m+1} = (\mathbb{V}_m \cup \{v_n\}, \mathbb{T}_m \cup \{t_l, t_r\})$  [Hop96]. Having  $v_a$  and  $v_b$  then  $v_l$  and  $v_r$  are determined in such a way that  $(|v_a| - |v_n|)^2$  is minimized after the split, with  $|v|$  denoting the valence of  $v$ .

#### 3.3. Half-Edge Collapse

An inactive neuron  $v_x$  and two triangles  $t_l, t_r$  can be removed from  $M$  by a half-edge collapse (cf. fig. 3). This operation is not guaranteed to preserve the topological type of  $M$ . Thus, removal of some  $v_x \in \mathbb{V}_x$  must be deferred until the respective collapse has become legal [HDD\*93].

For any mesh  $M_m = (\mathbb{V}_m, \mathbb{T}_m)$  a half-edge collapse  $c(v_n, v_a)$  is unambiguously defined by  $v_n, v_a \in \mathbb{V}_m$  as a transformation from  $M_m$  to a new mesh  $M_{m+1} = (\mathbb{V}_m \setminus \{v_n\}, \mathbb{T}_m \setminus \{t_l, t_r\})$ , if  $c$  is legal [Hop96]. Obviously split and collapse are invertible, so that  $s^{-1}(v_a, v_l, v_r, v_n) = c(v_n, v_a)$  and vice versa.

#### 3.4. Progressive Mesh

Hoppe presented a bottom-up method to find a sequence  $(o) = (s_0, s_1, \dots, s_{n-1})$  and a coarse triangle mesh  $M_0$  for any detailed triangle mesh  $M_n$  in such a way that  $M_n$  can be reconstructed from  $M_0$  by applying  $(o)$ :  $M_0 \xrightarrow{s_0} M_1 \xrightarrow{s_1} \dots \xrightarrow{s_{n-1}} M_n$ . Hoppe defined the tuple  $(M_0, (o))$  as a progressive mesh (PM) representation of  $M_n$  [Hop96] – a compact way to store any triangle mesh including level of detail.

#### 3.5. New Vertex Removal

Using GCS to reconstruct  $M'_n$  leads to a sequence  $(o') = (o'_0, o'_1, \dots, o'_{n-1})$  consisting of both, split and collapse operations. Thus,  $(M'_0, (o'))$  is no PM representation of  $M'_n$ , but very similar to such a representation. Level of detail (LOD)

**Figure 4:** Median running times of the new vertex removal (solid) compared to the classic half-edge collapse (dashed).

can still be achieved by subsequently applying the inverted split and collapse operations of  $(o')$  to  $M'_n = (\mathbb{V}'_n, \mathbb{T}'_n)$ . But during the LOD steps towards the coarser mesh, inverting any collapse operation  $c'_i \in (o')$  increases the number of vertices. Since these superfluous vertices do not belong to  $\mathbb{V}'_n$ , their position is undefined. To overcome this, we replace a half-edge collapse in GCS by a more general vertex removal in such a way that the neural network learns a PM representation, iteratively.

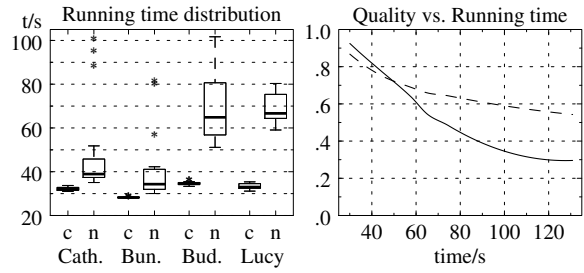
Until the first  $v_x$  has to be removed from a mesh  $M_m$ , only vertex splits have been performed and thus the corresponding operation sequence  $(o) = (s_0, s_1, \dots, s_k, \dots, s_{m-1})$  has been stored. Instead of adding another operation to  $(o)$  that removes  $v_x$  we want to find a sequence  $(o')$  not producing  $v_x$  from  $M_0$  in the first place, i. e., erase  $v_x$  from history.

Let  $s_k$  be the last operation in which  $v_x$  is involved either as  $v_a$  or  $v_n$ , then  $(o)$  can be rewritten as  $(o) = ((\underline{o}), s_k, (\bar{o}))$ . To remove  $v_x$  from  $M_m$  the inverted sequence  $(s_k, (\bar{o}))^{-1} = (s_{m-1}^{-1}, s_{m-2}^{-1}, \dots, s_{k+1}^{-1}, s_k^{-1})$  is applied to  $M_m$  simplifying it to  $M_k$ . If  $v_x$  was involved as  $v_n$  in  $s_k$  then  $v_x \notin \mathbb{V}_k$ , since  $v_x$  was removed by applying  $s_k^{-1}$ . Thus,  $v_x$  can be deleted.

If on the other hand  $v_x$  was involved as  $v_a$  in  $s_k$  then  $v_x \in \mathbb{V}_k$ , so it is still connected in  $M_k$ . Therefore,  $v_x$  must not be deleted. Instead  $v_n$  can be deleted since  $v_n \notin \mathbb{V}_k$  after applying  $s_k^{-1}$ . The attributes assigned to  $v_n$  must be preserved by transferring them to  $v_x$ , the neighbor of  $v_n$  in  $M_{k+1}$ . So, if  $v_x$  was involved as  $v_a$  in  $s_k$ , removal of  $v_x$  is replaced by removal of  $v_n$ . As a consequence every reference to  $v_n$  in the operations of  $(\bar{o})$  has to be replaced by a reference to  $v_x$ .

Special care must also be taken if no  $s_k$  exists, i.e.,  $v_x \in \mathbb{V}_0$  has not yet been involved as  $v_a$  or  $v_n$  in any split operation. In that case  $(o)$  can be rewritten as  $(o) = (s_0, (\bar{o}))$ , and  $(o)^{-1}$  must be applied to  $M_m$  simplifying it to  $M_0$  with  $v_x$  still connected. As in the previous case, attributes of another vertex ( $v_n$  of  $s_0$ ) must be transferred to  $v_x$ , the respective references in  $(\bar{o})$  have to be replaced, and the other vertex can be deleted.

Finally, the sequence  $(\bar{o})$  has to be reapplied to  $M_k$  to get back a detailed mesh  $M'_m$  reusing the original attributes from  $\mathbb{V}_m$  with one caveat: Since a vertex has been deleted,  $v_l$  or  $v_r$  might have become invalid for some  $s_i = s(v_a, v_l, v_r, v_n) \in (\bar{o})$ . Thus, some  $s_i$  have to be repaired. A straight-forward



**Figure 5:** Reconstruction of 10,000 vertices. Left: Running times of algorithm using half-edge collapse (c) and new vertex removal (n). Right: Quality vs. running time for a reconstruction of 10,000 vertices in terms of ratio of valence 5-7 vertices (dashed) and Delaunay triangles (solid) for the combined results of all four meshes.

repair is to identify a neighboring vertex  $v_b$  of  $v_a$  minimizing the angle  $\angle v_b v_a v_n$ . Thus,  $v_n$  is near to the edge  $v_a, v_b$ . Finally,  $v_l$  and  $v_r$  can be determined as in subsection 3.2.

Let  $M_c = (\mathbb{V}_c, \mathbb{T}_c)$  be the mesh produced by removing  $v_x$  from  $M_m$  by a half-edge collapse and  $M'_m = (\mathbb{V}'_m, \mathbb{T}'_m)$  be the mesh produced by removing  $v_x$  from  $M_m$  with the new technique. Then  $|\mathbb{V}'_m| = |\mathbb{V}_c|$  and  $|\mathbb{T}'_m| = |\mathbb{T}_c|$  with  $|\cdot|$  denoting the number of elements in a set. Furthermore, the learned attributes associated to the vertices in  $M'_m$  are the same as those of  $M_c$ . So,  $M'_m$  is similar to  $M_c$  and the sequence  $(o') = ((\underline{o}), (\bar{o}))$  is the one we had to find. By construction all operations of  $(o')$  are splits, and thus the tuple  $(M_0, (o'))$  is a progressive mesh representation of  $M'_m$ .

## 4. Results

The presented algorithm was tested in a single thread on an Apple MacBook Pro, 2.66 GHz Intel i7 CPU, 8 GB RAM. Meshes were reconstructed from four point clouds: Bunny, Happy Buddha and Lucy, obtained from the Stanford scanning repository, and a synthetic model of the cathedral of Paderborn, Germany. Each reconstruction was tested with 15 different random seeds. To address runtime effects each test was repeated four times to determine mean reconstruction times and quality measures for the respective seed.

### 4.1. Reconstruction Times

The proposed technique does not impose severe running time overhead for the cathedral and Bunny (cf. fig. 4). When reconstructing a triangle mesh of 10,000 vertices, median running times increased from 32.0 s using half-edge collapse to 38.9 s using new vertex removal for the cathedral and from 28.2 s to 34.3 s for Bunny. When reconstructing meshes with very fine details, median running times increased from 34.4 s to 64.9 s for Buddha and from 33.0 s to 66.7 s for Lucy.

The new technique leads to a greater variation of running

**Table 1:** Mesh Quality after reconstructing 10,000 vertices

Mesh	Valence 5-7		Delaunay		Hausd. Dist.	
	old	new	old	new	old	new
Cathed.	79 %	77 %	86 %	82 %	1 %	3 %
Bunny	87 %	84 %	91 %	89 %	3 %	4 %
Buddha	73 %	66 %	80 %	57 %	3 %	2 %
Lucy	78 %	64 %	85 %	50 %	4 %	7 %

times for different random seeds (cf. fig. 5 left). Nevertheless, running times for Cathedral, Bunny and Lucy do not deviate as much from the respective median time than the running times for Buddha do – a mesh not homeomorphic to the others.

#### 4.2. Mesh Quality

Quality of the reconstructed meshes was evaluated in terms of regularity, i. e., the ratio of vertices with valence 5 to 7 and the ratio of triangles fulfilling the Delaunay criterion. The new technique reduces mesh quality of the reconstructed mesh only slightly for the cathedral and Bunny (cf. tab. 1) and moderately for Buddha and Lucy.

Hausdorff distances were determined between each reconstruction and the respective triangle mesh from which the point cloud was generated. With both, the old and our new technique, similarly small Hausdorff distances were achieved (cf. tab. 1, normalized to the diagonal of the bounding box).

During vertex removal, sequences  $(s_k, (\bar{o}))$  need to be reverted and reapplied. Short running times for a fixed number of reconstructed vertices indicate that those sequences are short whereas long running times indicate that those sequences are long. From fig. 5 right it can be seen that quality gets reduced for longer sequences. However, short sequences  $(s_k, (\bar{o}))$  exist for many different random seeds resulting in good mesh quality. A visual example of the quality of the reconstructed mesh is shown on the far left of fig. 1.

#### 4.3. Level of Detail

At any time, the reconstructed mesh can be reduced to a coarser mesh using the automatically learned level of detail (LOD) steps while preserving the shape of the reconstructed object with good visual quality. Fig. 1 shows an LOD sequence for Stanford Bunny reducing a mesh of 20,000 triangles to a coarser mesh of 312 triangles.

#### 4.4. Memory Requirements

In a reconstructed triangle mesh  $|\mathbb{T}| \approx 2|\mathbb{V}|$ ,  $|(o)| \approx |\mathbb{V}|$ . Assuming that an index to a vertex consumes the same amount of memory as a vertex' component, an indexed triangle list for the reconstructed 3D mesh  $M$  needs  $3|\mathbb{V}| + 3 \cdot 2|\mathbb{V}|$  units of memory. A progressive mesh representation of  $M$  needs only 66 % of that, i. e.,  $3|\mathbb{V}| + 3|\mathbb{V}|$  units of memory.

## 5. Conclusion and Future Work

We have successfully modified surface reconstruction based on Growing Cell Structures in such a way that the reconstructed triangle mesh is directly represented as a progressive mesh. The running time overhead of the new technique is related to the complexity of the final mesh but typically low. The new technique allows for level of detail and compact storage and transfer while preserving a good mesh quality.

We plan to use the progressive mesh representation for transfer and visualization in the processing pipeline of the AVIGLE project. Furthermore we will investigate how to utilize the integrated level of detail in the triangle mesh rendering step to improve the rendering times.

Finally we plan to integrate recent improvements to GCS like [AB10] into our new system.

#### Acknowledgements

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