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# 3D for all!

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# Compressing and simplifying complex 3D polyhedra

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# What motivates you?

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- ◆ Problem solving pleasures?
- ◆ Peer recognition?
- ◆ A hunger for knowledge?
- ◆ The need to impact society?

# A vision for GVU

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- ◆ Invent technologies that will make humans more effective in their professional, scholastic, and private activities
- ◆ Teach objectives, motivation, creativity, teamwork... the theory... and Java3D
- ◆ Work with industrials to understand where they are coming from and to help them decide where to go

# How do we get there?

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- ◆ **Study humans and organizations**
  - Activities/needs
  - Capabilities/limitations
- ◆ **Explore technologies and inventions**
  - R&D strategies and invention history
  - State-of-the art, possibilities, limitations
  - Hands-on experience/use what you create
- ◆ **Understand commercialization**
  - Market forces and acceptance issues
  - Engineering and testing for usability
  - Development and maintenance

# Some Examples

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- ◆ **Multimedia capture of courses**
- ◆ **Mobile visual communication devices**
- ◆ **Intelligent appliances**
- ◆ **VR treatment of phobia**
- ◆ **Collaborative CAD**
- ◆ **Data mining**
- ◆ **Visualization**

# **How big is 3D graphics?**

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- ◆ **All graphic adaptors will be 3D enabled**
- ◆ **Next “must” after mouse, color, www**
- ◆ **Perspective = Detail + Background**
- ◆ **Intuitive**
- ◆ **Appealing**
- ◆ **Drives huge markets**

# What is it good for?

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- ◆ **3D models of**
  - **terrain, underground cavities**
  - **homes, offices, buildings, cities**
  - **factories, assembly lines, robots**
  - **airplanes, cars, ships**
  - **consumer products**
  - **human organs, molecules**
  - **engineering simulation results**
  - **avatars, shopping malls, enemies**



# Why would I use it?

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- ◆ Games, electronic commerce
- ◆ Design, PDM
- ◆ Design review, ergonomics
- ◆ Bids/part catalogs
- ◆ Communication/marketing
- ◆ Data understanding
- ◆ Intuitive navigation/selection
- ◆ Training/therapy

# Why can't I?

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- ◆ **Complex models**
- ◆ **Accessed through internet/phone**
- ◆ **Slow connections**
- ◆ **Limited rendering speed and storage**
- ◆ **Difficult user interface**

# What is a 3D graphic model?

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- ◆ Representation of 3D geometry
- ◆ Surfaces and lighting model
- ◆ 3D images, textures
- ◆ Sampling of 4D light field
- ◆ Procedure + parameters for 3D graphics

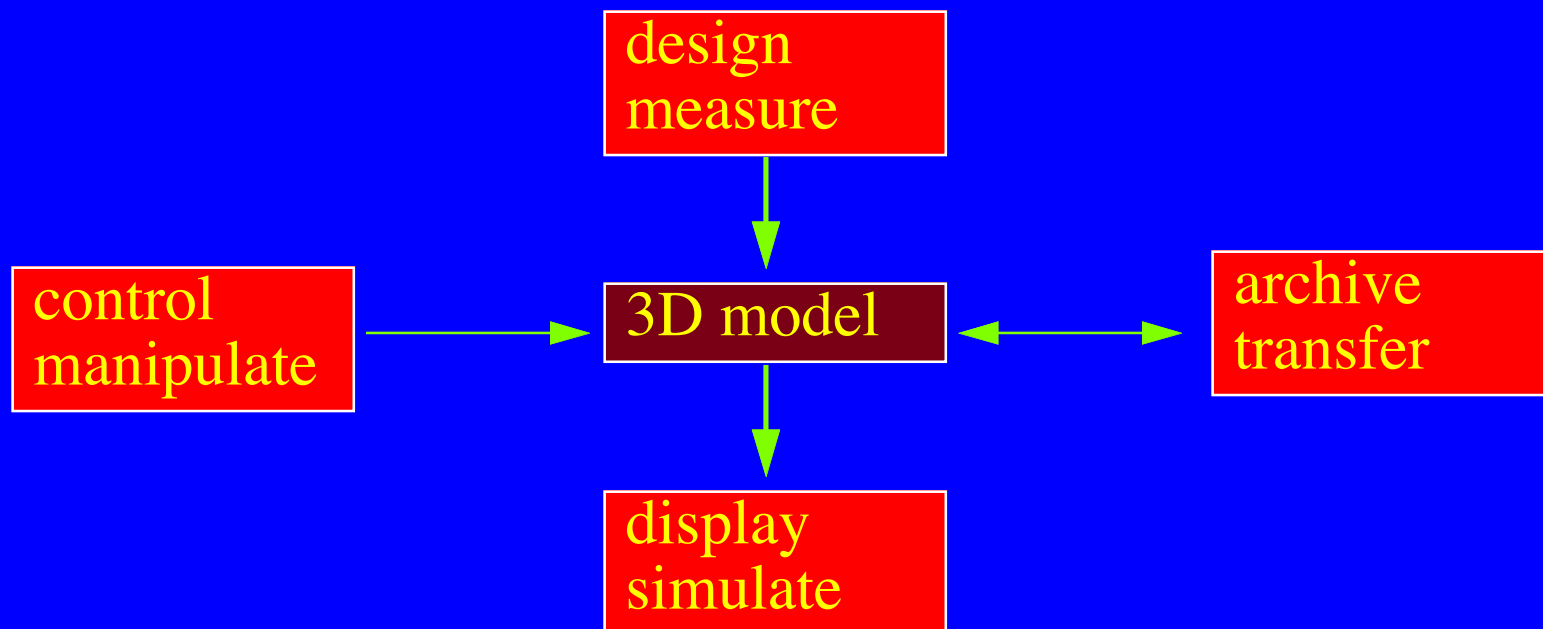
# What is a 3D graphic application?

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## ◆ Representation

- Geometry: vertex coordinates
- Topology: triangle/vertex incidence
- Photometry: colors, normals, textures

## ◆ Architecture of a 3D system



# **What makes it effective?**

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- ◆ **Fast access to 3D databases**
- ◆ **Internet connectivity**
- ◆ **Intuitive view and model manipulation**
- ◆ **Realtime feedback**

# The human needs?

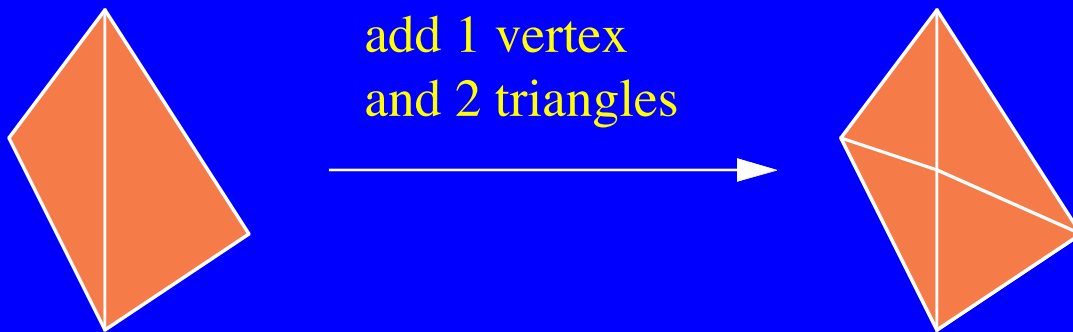
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- ◆ **I want to access the data!**
  - Compression
  - Progressive transmission
- ◆ **I want to see what I am doing!**
  - Simplification, graphic acceleration
- ◆ **I want to be in control!**
  - Virtual camera

# Why focus on triangles?

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- ◆ **Optimized rendering systems**
- ◆ **Easily derived from polygons and surfaces**
- ◆ **Good measure of graphic complexity**
  - Twice more triangles than vertices



# How many do you need?

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- ◆ A sphere=12x24x2 triangles
- ◆ Airplane=50,000,000 triangles
- ◆ A city?
- ◆ A human body?



# How much space do they take?

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- ◆ **Geometry: 3 coordinates per vertex**
- ◆ **Topology: 3 vertex indices per triangle**
- ◆ **Photometry: Normals, textures, colors**
- ◆ **Total: up to a 100 bytes per triangle**

# Is that a problem?

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- ◆ **A 100MT model takes:**
  - A month to download over the phone
  - An hour to display
- ◆ **Complexity will grow faster than bandwidth and graphic performance**

# How to cope with this complexity?

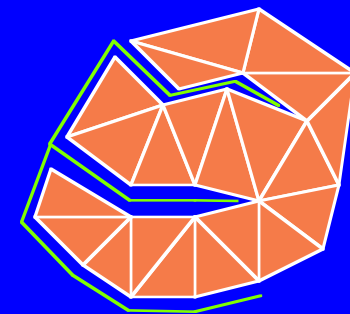
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- ◆ Don't bother with unimportant details
- ◆ Compress
  - Helps with transfer, storage, paging
- ◆ Eliminate redundant graphic operations
  - Visibility, back-face culling, triangle-strips
- ◆ Trade accuracy for performance
  - Lossy compression, simplification, images

# How good is compression?

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- ◆ **Lossless compression**
  - Preserves geometry and topology
  - Reduces # of bits for triangle/vertex incidence
  - Does not compress vertex representation
- ◆ **Current approach (Taubin&Rossignac)**
  - Cut surface into tree of corridors
  - Encode internal triangulation of corridors
  - 1.2 to 2.2 bits per Triangle
  - plus the vertex coordinates



# Do I need full numeric accuracy?

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- ◆ **Models are approximations anyway**
  - Imprecise measures or toleranced dimensions
  - Limited accuracy in geometric computation
  - Truncated coordinates to nearest float or double
- ◆ **Use very short integers!**
  - **Floats are bad for geometry**
    - » Accuracy grows with distance to origin
    - » Geometric models need uniform accuracy
  - **Integers are perfect**
    - » Uniform accuracy through out the model
    - » More precise than floats for same number of bits
  - **Don't need 32 bits**
    - » 11 bits: 1/2mm for an engine block

# Can this save more storage?

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- ◆ **Lossy compression**
  - shorter representations of vertex coordinates
  - more frequent repetitions of values
  - efficient entropy coding schemes
- ◆ **Current approach (Taubin&Rossignac)**
  - Quantize vertex coordinates to 8-12 bits
  - Predict location of next vertex
  - Code difference (short corrective vector)
  - Use variable length coding (entropy)
  - Compresses down to about 6 b/T

# Do I need all these triangles?

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- ◆ **Can't see most of them**
  - quickly discard invisible ones
- ◆ **Many details are smaller than a pixel**
  - remove them or use an impostor
- ◆ **Surface tessellations are not optimal**
  - Need accuracy at silhouettes
  - Could use coarser meshes elsewhere

# How do I take advantage of this?

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- ◆ **Precompute approximations of features:**
  - surface subsets, objects, groups
- ◆ **Use approximations to accelerate graphics**
  - when resulting visual error acceptable
- ◆ **Current approaches**
  - **Coalesce clusters of vertices**
    - » How to form the clusters' hierarchy?
    - » Where to place the result of coalescing a cluster?
  - **Remove degenerate triangles**
  - **Dynamically select LOD based on view**
    - » How to measure error?
    - » How to allocate rendering time?
    - » How to avoid artifacts?



# Do I need training to use 3D?

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- ◆ **Why should you? Your kids got none..**
- ◆ **Few designers/many users**
  - **Scientists, doctors**
  - **Non technical professionals**
  - **Home shoppers**
  - **Game players**

# How do I control the view?

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- ◆ You don't want a HMD
- ◆ You can't afford a CAVE
- ◆ The track ball will break your... enthusiasm
- ◆ The mouse is not intuitive
- ◆ Use a virtual camera!

# What is a virtual camera?

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- ◆ 3D model
- ◆ (Large) screen
- ◆ Table with drawing or global view
- ◆ Move small camera over the table
- ◆ See in 3D what you are pointing at

# Outline of the presentation

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- ◆ **Geometric and topological compression**
  - Taubin&Rossignac
- ◆ **Grid-based vertex coalescence**
  - Rossignac&Borrel
- ◆ **Edge-collapse vertex coalescence**
  - Ronfard&Rossignac
- ◆ **Real icon for a virtual camera**
  - Rossignac&Wolf

# How do I measure the error?

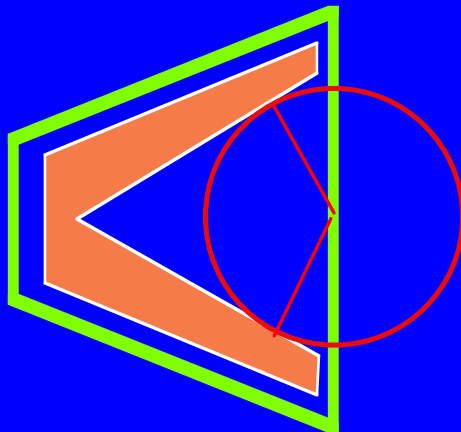
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- ◆ **Geometric 3D deviation**
  - View-independent
  - Allowed by model tolerance
- ◆ **Image space error**
  - View-dependent
    - » Silhouettes, color/shading variation
  - Bounded by projection of 3D error
- ◆ **Color error**
  - View dependent
  - Error on color reflected by surface point
  - Depends on surface orientation
  - Not important for most applications

# Hausdorff error

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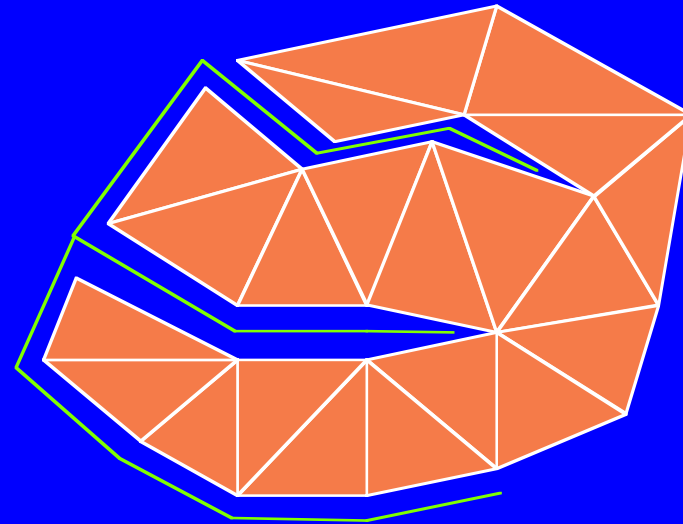
- ◆  $H(A,B) = \max(d(a,B), d(b,A))$ 
  - for all  $a$  in  $A$  and  $b$  in  $B$
- ◆ Radius of largest ball
  - that has its center on one surface and
  - that is disjoint from the other surface
- ◆ Expensive to compute
  - Need not happen at vertex or edge



# 3D Compression

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- ◆ **Geometric Compression through Topological Surgery**
  - Gabriel Taubin and Jarek Rossignac
  - IBM Research Report RC 20340,
  - Revised 7/1/97



# Mesh representations and storage

	vertex 1	vertex 2	vertex 3
Triangle 1	x y z	x y z	x y z
Triangle 2	x y z	x y z	x y z
Triangle 3	x y z	x y z	x y z

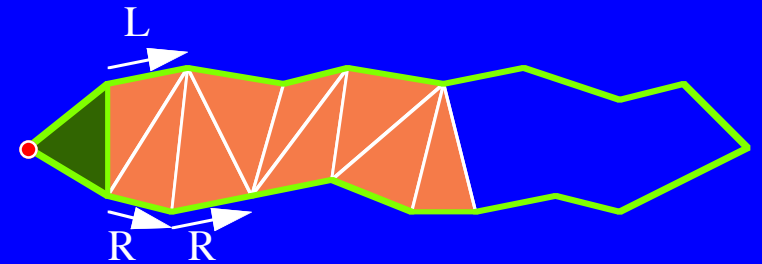
Independent triangles: **36 B/T**  
 -  $9 \times 4 \text{ B/T}$

Triangle 1	1 2 3	vertex 1	x y z
Triangle 2	2 3 4	vertex 2	x y z
Triangle 3	3 5 1	vertex 3	x y z

Vertex and mesh tables: **18 B/T**  
 -  $3 \times 4 \text{ B/V} + 3 \times 4 \text{ B/T}$

vertex 1	x y z	Strip 1	10
vertex 2	x y z	Strip 2	7
vertex 3	x y z		

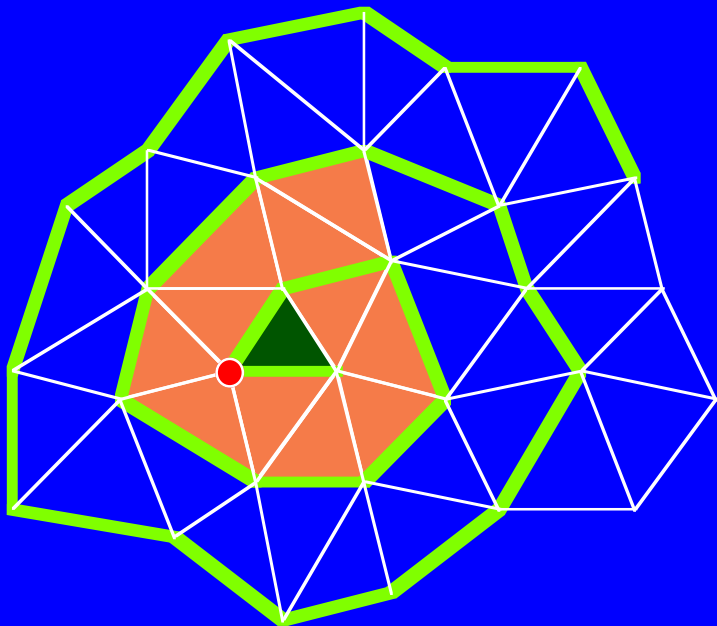
Triangle strips: **13.4 B/T**  
 -  $1.1 \times 3 \times 4 \text{ B/T} + 1 \text{ B/S} + 1 \text{ b/T}$





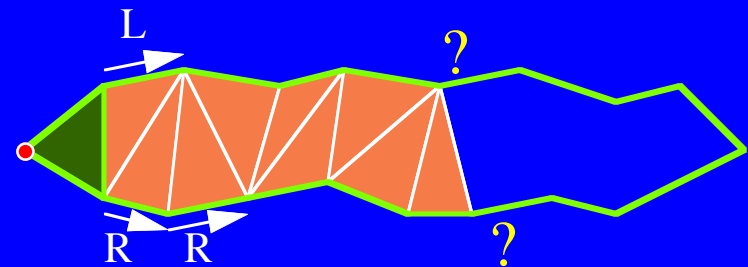
# Constructing and encoding corridors

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Connecting vertices in a spiral cut defines the boundary of a corridor (both sides).

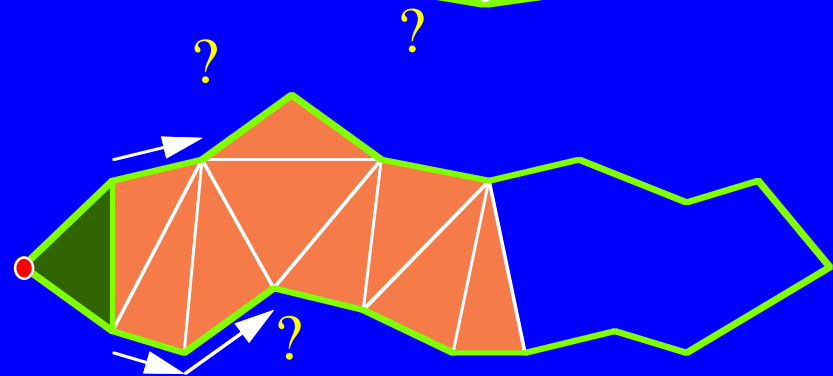
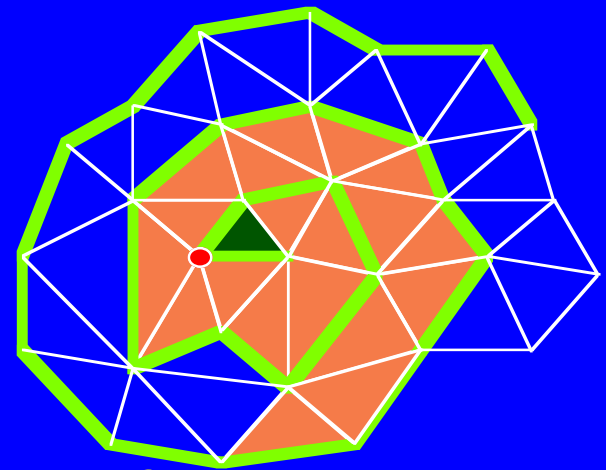
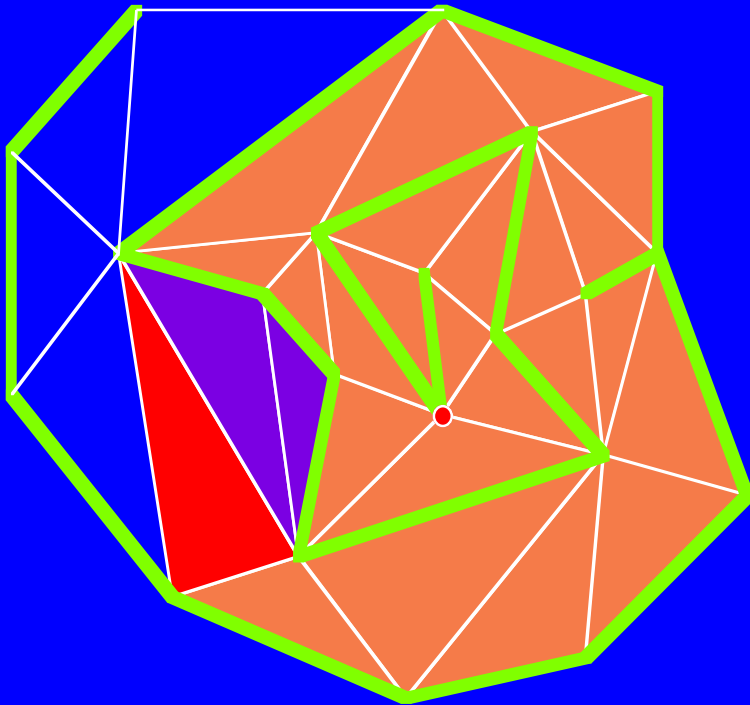
Given the boundary and the starting point, we need 1 bit/triangle to encode a strip



Store vertices in their order along the spiral  
Store one L/R bit per triangle (except first)

# Wait a minute!

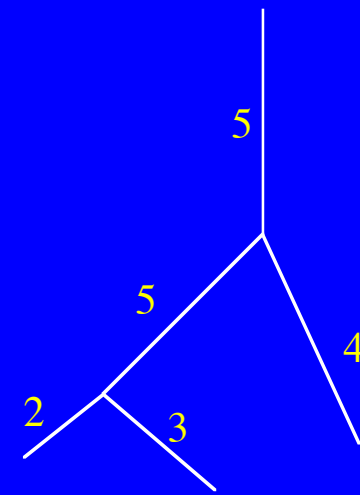
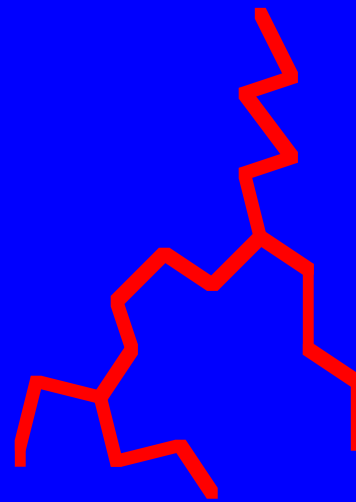
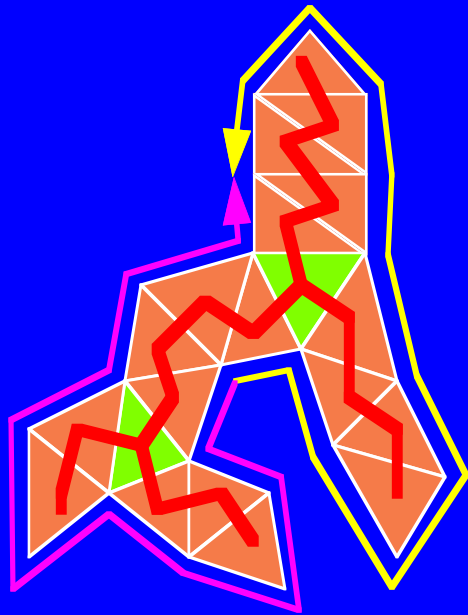
- ◆ The corridor may have warts!
- ◆ The spiral may cut itself or split!
- ◆ The corridor may bifurcate!



# Compression details

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- ◆ **Compress trees using runs**
  - Cut = Vertex spanning tree (zipper)
  - Corridors = Dual binary tree
- ◆ **Encode interior triangulation of corridor**
  - 1 bit per triangle



# Lossy geometric compression

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- ◆ **Quantize all vertex coordinates**
  - Desired precision
  - Consistent with modeling tolerance
- ◆ **Use tree ancestors to predict next vertex**
  - Optimal linear combination of ancestors
  - Store corrective vectors (error)
- ◆ **Use variable length coordinates**
  - Coordinates of correction are small integers
  - Lots of values repeated for complex models
  - Use short codes to frequently used values
  - Need between 3 and 10 B/T
    - » depending on tolerance

# Implementation

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- ◆ **VRML-2 compression/decompression**
  - **G. Taubin, P. Horn, F. Lazarus (IBM)**
  - **Compressed models: average of 1 B/T**
    - » **Depends on complexity, smoothness, tolerance**
    - » **Example: 160K triangle model**
      - ◆ **Tolerance: 0.0005 of model size (11 bit quantization)**
      - ◆ **Incidence: 1.2 b/T**
      - ◆ **Geometry: 5.4 b/T**
  - **Decompression speed: 60K T/sec**

# Other compression techniques

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- ◆ **Deering (Siggraph'95)**
  - **Extend triangle strip**
    - » Maintain buffer of 16 vertices for reuse
    - » Op-code for building next triangle: 4-6 b/T
    - » Vertex quantization and variable length coding
      - ◆ Local coordinate system
  - **Good for graphics:**
    - » In-line fast decoding and small local storage
- ◆ **Hoppe (Siggraph'96)**
  - **Store vertex-split operations**
    - » Index to vertex
    - » Index to 2 adjacent edges
    - » Displacement(s) from common vertex to new pair
      - ◆ Short vectors (variable length coding)

# Model simplification

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- ◆ **Multi-resolution 3D approximations for rendering complex scenes**
  - Jarek Rossignac and Paul Borrel
  - Geometric Modeling in Computer Graphics'93
- ◆ **Full-range approximations of triangulated polyhedra**
  - Remi Ronfard and Jarek Rossignac
  - Eurographics'96 (Computer Graphics Forum)

# Multi-resolution models

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- ◆ **Show distant features at lower resolution**
- ◆ **Split the model into small features**
  - Use design entities (solids or groups)
  - Split large and complex solids
- ◆ **Precompute several levels of detail per feature**
  - Logarithmic reduction of triangle count
  - Guaranty error bound
- ◆ **Select appropriate resolution for each feature**
  - Perspective projection of error estimate
  - Position on screen, velocity
- ◆ **Merge groups of small distant features**
  - Preserve overall volume and color?



# Vertex merge (Rossignac&Borrel)

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- ◆ **Cluster vertices using grid**
  - Compute truncated coordinates for each vertex
  - Use them as a cluster identifier
- ◆ **Coalesce vertex clusters**
  - Compute location of representative vertex
  - Associate each vertex with its new location
- ◆ **Remove degenerate triangles**
  - Those with 2 or 3 vertices in the same cluster
- ◆ **Build display lists for each LOD**
  - New/old normals and textures
  - Triangle strips

# Pros and cons for Rossignac&Borrel

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## ◆ Advantages

- Much faster than any other method
- Very robust (no restriction on input data)
- Simple code (implement in hours)
- Guaranteed error bound (cell diagonal)
- Reduces topological complexity (holes...)
- Very effective for complicated details
- Does not create holes or gaps in surface

## ◆ Drawbacks

- Suboptimal for simplifying smooth flat surfaces
  - » A vertex cannot travel more than the cell size
- Simplified surface may self intersect
- Hard to achieve precise triangle count

# Extensions and variations

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- ◆ **Low&Tan, Interactive 3D Graphics'97**
  - Sort vertices by importance in each cell
  - Attract vertices from neighboring cells
- ◆ **Luebke&Erikson, Siggraph'97**
  - Octree or other vertex clustering technique
  - Hierarchy of clusters
  - View defines which clusters are active
  - List of active triangles
  - Temporal coherence for adaptive LOD
  - Bad for T-strips and display lists
  - Use only for large, complex solids
- ◆ **Popovic&Hoppe, Siggraph'97**
  - Combine PM with Rossignac-Borrel's proximity

# Edge collapse (Ronfard&Rossignac)

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- ◆ **Coalescence vertices**
  - that are further apart than the tolerance
  - as long as they slide close to the surface
- ◆ **Efficient error estimate for a cluster**
  - Max distance between representative vertex and all the planes supporting the incident triangles upon the vertices of the cluster
- ◆ **Approach**
  - Evaluate error associated with edge collapses
  - Maintain sorted list of candidate edges
  - Keep collapsing edges until reach
    - » tolerance or
    - » desired triangle count

# Pros/cons for Ronfard&Rossignac

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## ◆ Advantages

- Better simplification ratios for same tolerance
- Can control error or triangle count
- Can choose whether to preserve topology or not

## ◆ Drawbacks

- Requires maintaining incidence graph
- Imposes topological restrictions on data
- Slower than grid-based coalescence
- Hard to achieve precise triangle count

# Extensions and variations

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- ◆ **Garland&Heckbert, Siggraph'97**
  - Use least square distance to supporting planes
  - Propagate only 4x4 matrix instead of all planes
  - Not a bound on the error!
- ◆ **Hoppe, Siggraph'96**
  - Store sequence of edge collapse operations
  - Use it's inverse as a progressive mesh (PM)
  - Each split is defined by
    - » 2 adjacent edges in the previous model
    - » The relative position of the 2 new vertices

# Conclusion

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- ◆ **Increasingly complex triangular 3D models**
- ◆ **Compress, simplify within tolerance**
- ◆ **Bit-efficient coding: 1 Byte/triangle**
- ◆ **Simplification for fast graphics:**
  - **Grid-based vertex coalescence**
    - » **Fast, robust, effective, suboptimal**
  - **Edge-collapse**
    - » **Slower, more precise, better results**
- ◆ **Need extractable encoding for**
  - **view-dependent multi-res transmission**